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# Hybrid and Kinetic Simulations of Particle Dynamics in Coaxial Plasma Jet Accelerators\*

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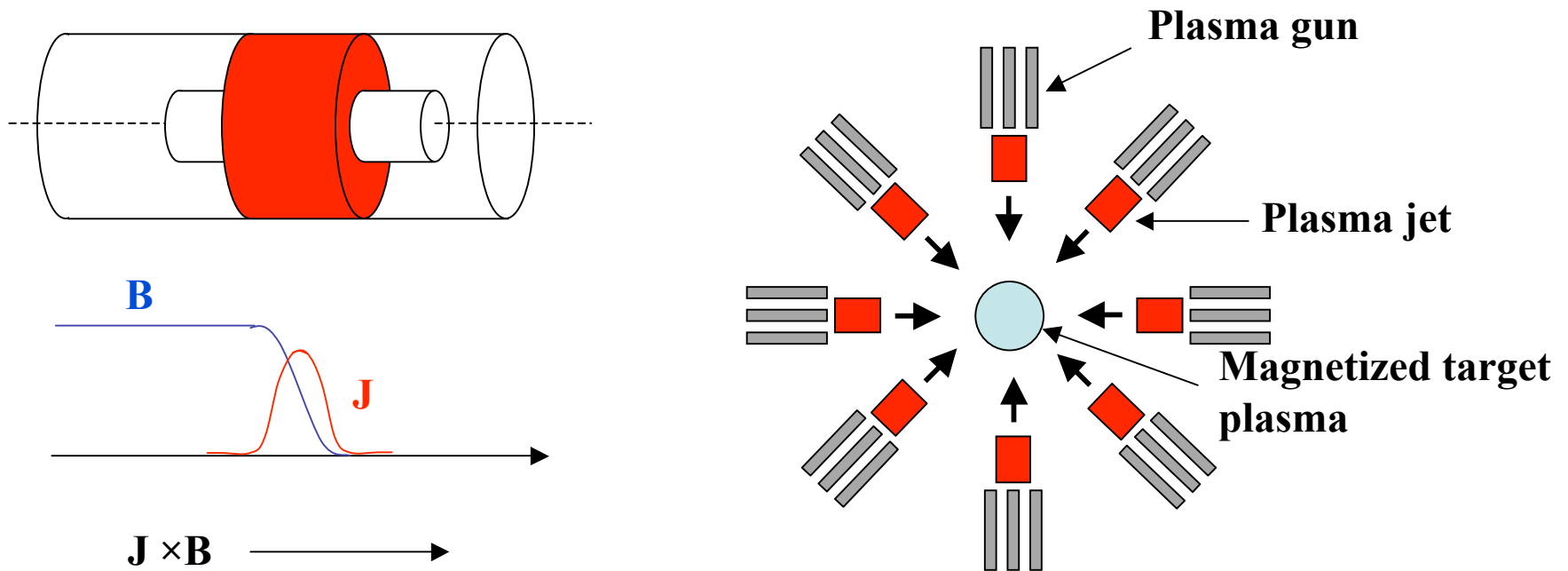
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\*Work supported by DOE Office of Fusion Energy Science through HyperV Technologies Corp.

# Topics

1. Motivation: Application of plasma jets to Magnetized Target Fusion
2. EMHD and Collisional PIC Algorithms for Plasma Jet Simulations
3. Multi-species acceleration in 1D
4. 2D coaxial simulations
5. Conclusions and Future Work

# Coaxial plasma jets: Drivers for Magnetized Target Fusion (MTF)



Coax length  $\sim 1$  m

Deuterium plasma “slug”  
( $\sim 10^{17}$  /cm<sup>-3</sup>) accelerated to  
velocities  $\sim 200$  km/s in a  
few  $\mu$ s.

MTF: Plasma jets merge to form an  
imploding liner. \*

\*Y.C.F. Thio *et al*, Journal of Fusion Energy **20** 1 (2002)

# EMHD and Kinetic PIC Algorithms in LSP

## EMHD:

Drop electron inertia: **Do not have to resolve fast electron time-scales**

Ion species treated kinetically (including ion-ion collisions);

Electric field obtained from generalized Ohm's law.

**EMHD algorithm uses constant  $\sigma$  calculated from initial values of  $T_e$  and  $n_e$**

$$\sigma = \frac{n_e e^2}{m_e \nu_{ei}} \propto T_e^{3/2}$$

## Implicit Kinetic PIC:

At somewhat lower densities can run fully kinetic simulations using Direct Implicit model in LSP\*.

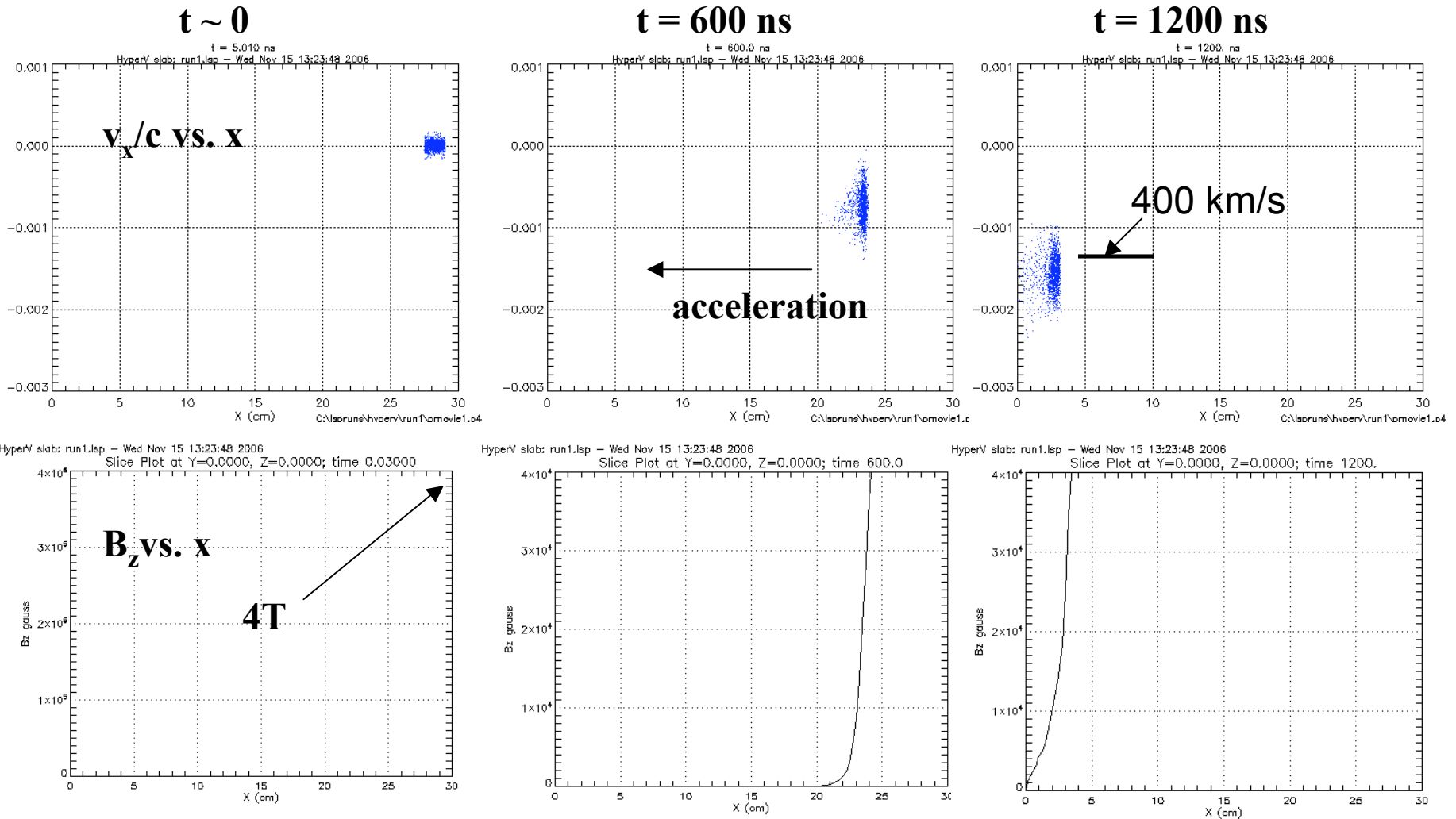
Spitzer collision model for electrons and ions

\* D.R. Welch, D.V. Rose, M.E. Cuneo, R.B. Campbell, and T.A. Mehlhorn, Phys. Plasmas 11, 751 (2004)

# EMHD simulation of plasma jet acceleration in $1.2\mu\text{s}$

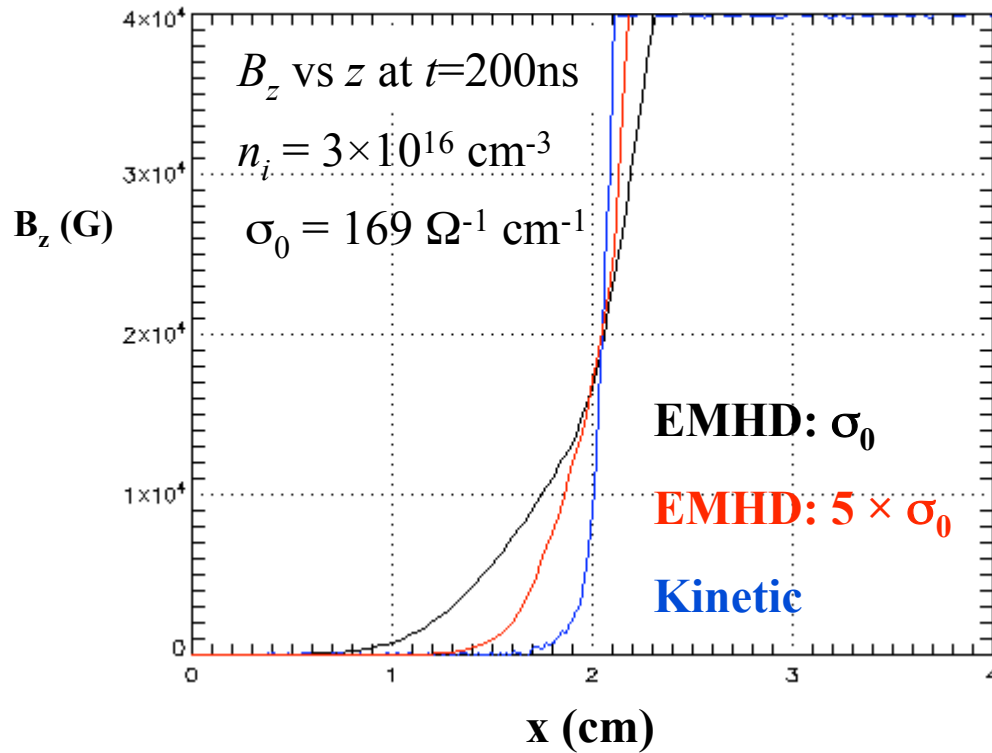
$$n_i = 3 \times 10^{17} \text{ cm}^{-3} \quad (\rho = 10^{-6} \text{ g/cm}^{-3}) \text{ Deuterium}$$

$$T_i = 5 \text{ eV} = T_e$$



**Propagates 30 cm in  $1.2 \mu\text{s}$ , in agreement with slug model.  
Some axial heating of ions is seen**

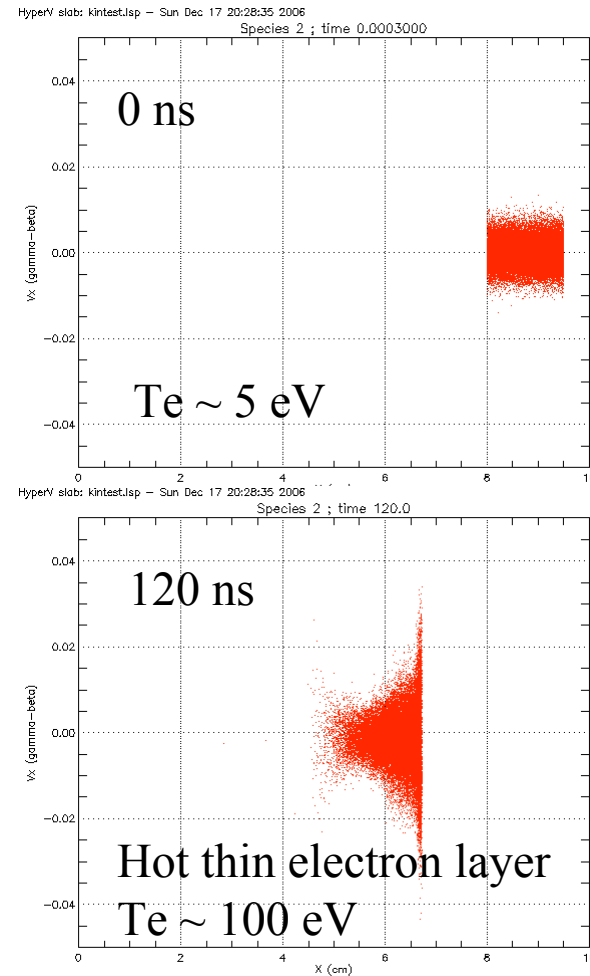
# Kinetic diffusion layer thinner than EMHD layer due to large electron heating



Diffusion layer gets thinner for EMHD simulation with increased conductivity

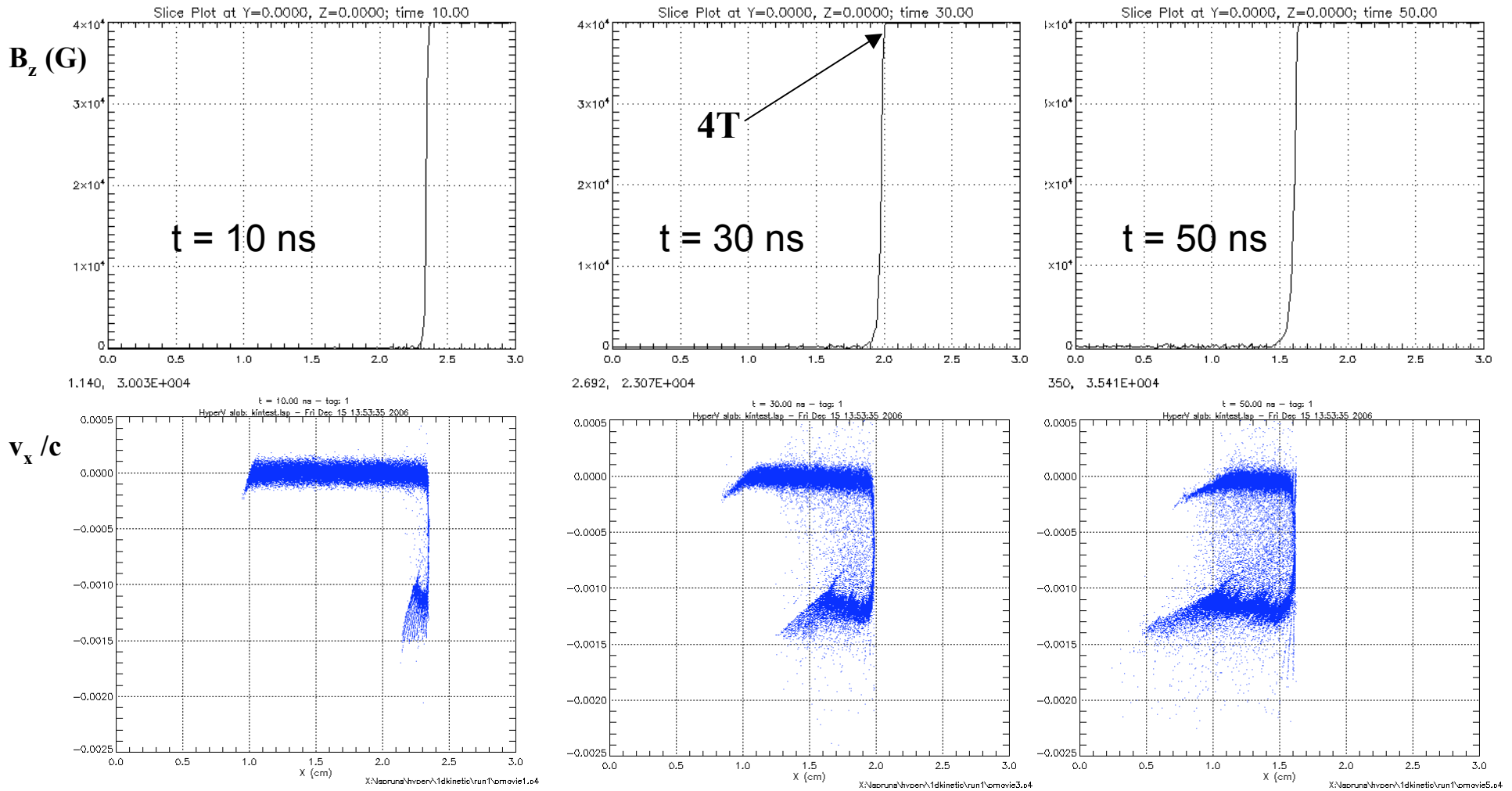
$$\sigma \propto T_e^{3/2}$$

## Electron phase-space



Increased local conductivity

For large fields ions accelerated ballistically in thin diffusion layer



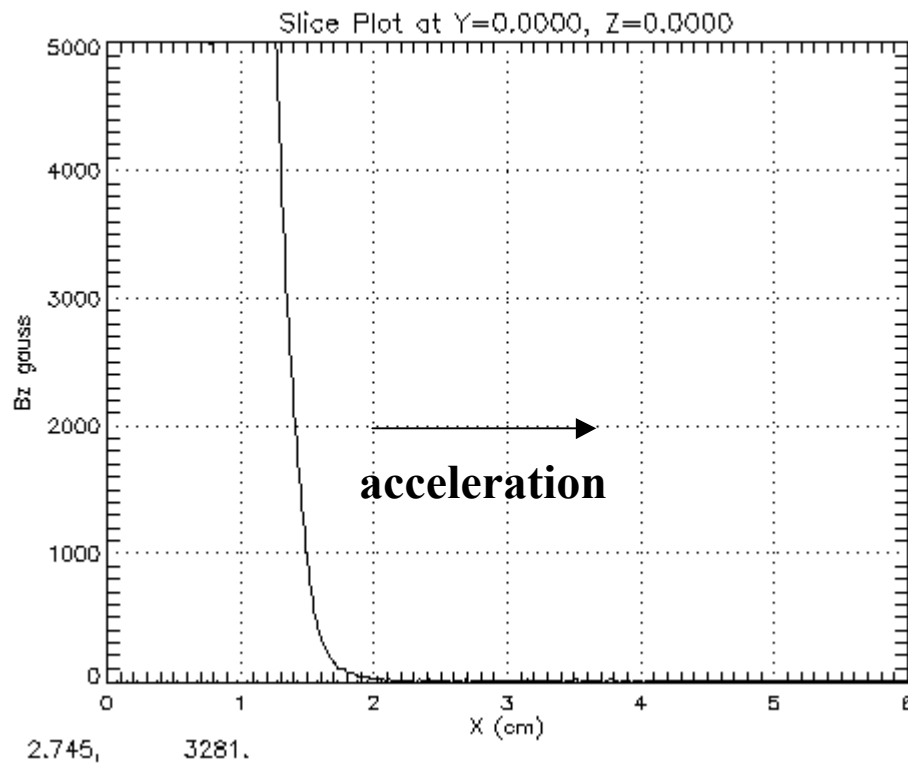
**Accelerated ions have much increased mean-free-path  
Ion-ion collisions “fill-in” the phase-space**

# Different ion dynamics at lower field values

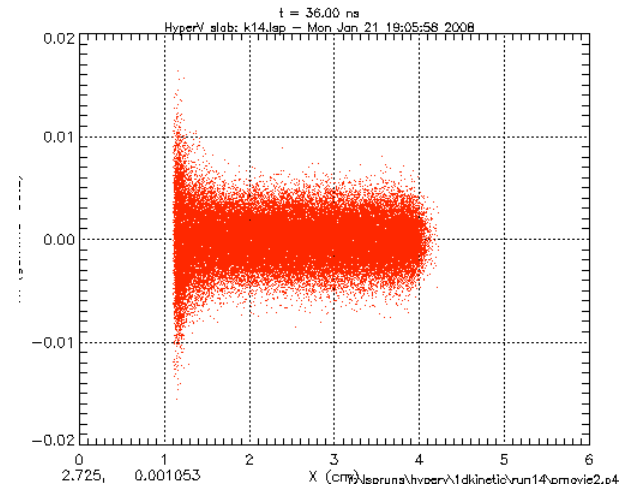
$$B_z = 0.5 \text{ Tesla}$$

$$n_i = 10^{16} \text{ cm}^{-3} \text{ Deuterium}$$

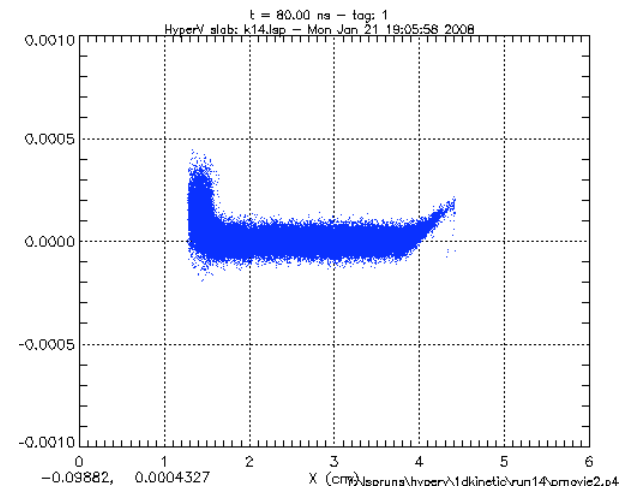
$$T_i = 5 \text{ eV} = T_e$$



**Thicker diffusion layer**



**Less ohmic heating of electrons**



**Ions collisional in sheath**

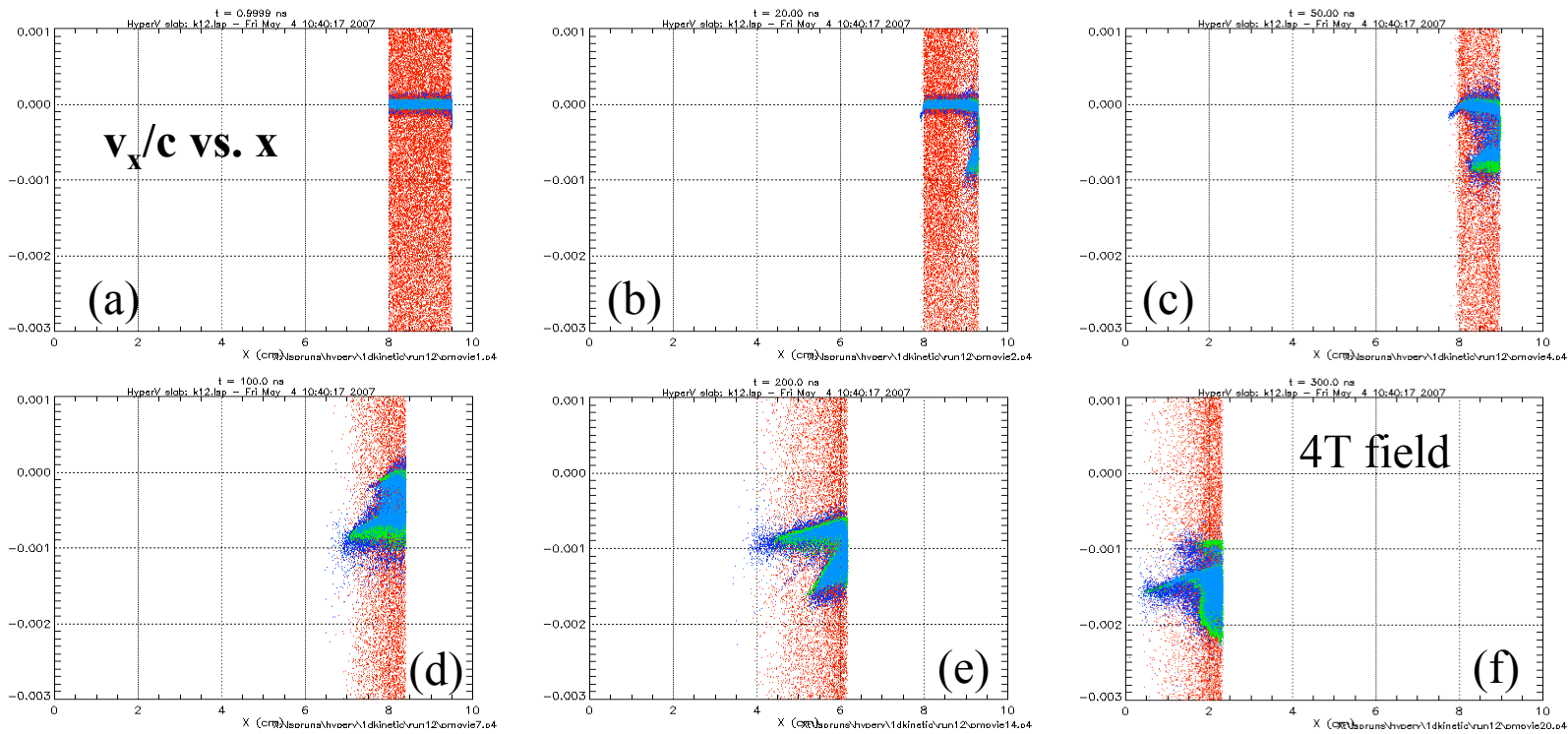


# Acceleration of mixed-species jet

HyperV jet is composed of 2 parts Hydrogen to 1 part Carbon

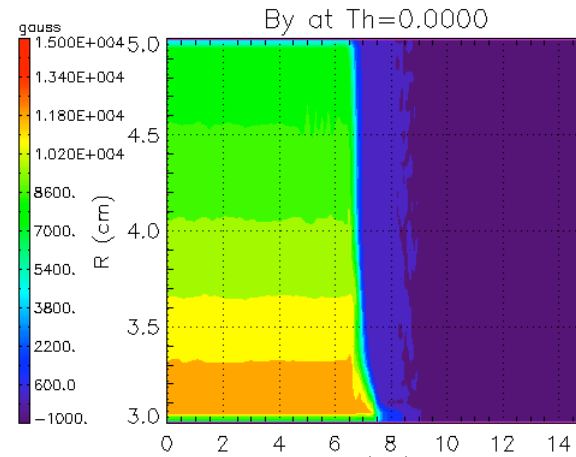
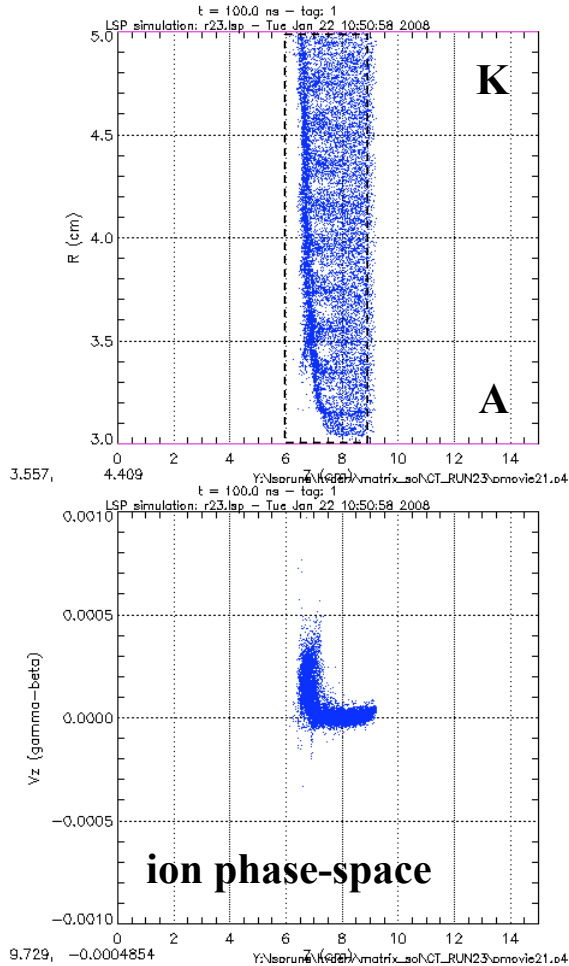
**Simulations show mixture remains relatively homogeneous**

$e^- : n = 3.5 \times 10^{16} \text{ cm}^{-3}$   
 $D^+ : n = 2 \times 10^{16} \text{ cm}^{-3}$   
 $C^+ : n = 0.5 \times 10^{16} \text{ cm}^{-3}$   
 $C^{2+} : n = 0.5 \times 10^{16} \text{ cm}^{-3}$

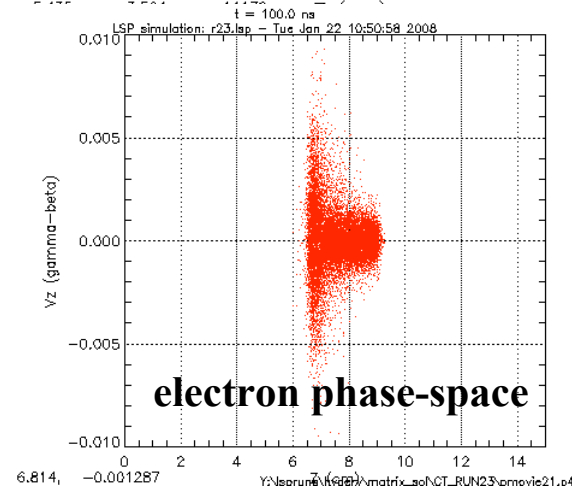


$t =$  (a) 1 (b) 20 (c) 50 (d) 100 (e) 200 (f) 300 ns

# 2D cylindrical coax simulations undertaken to investigate modifications to 1-D predictions



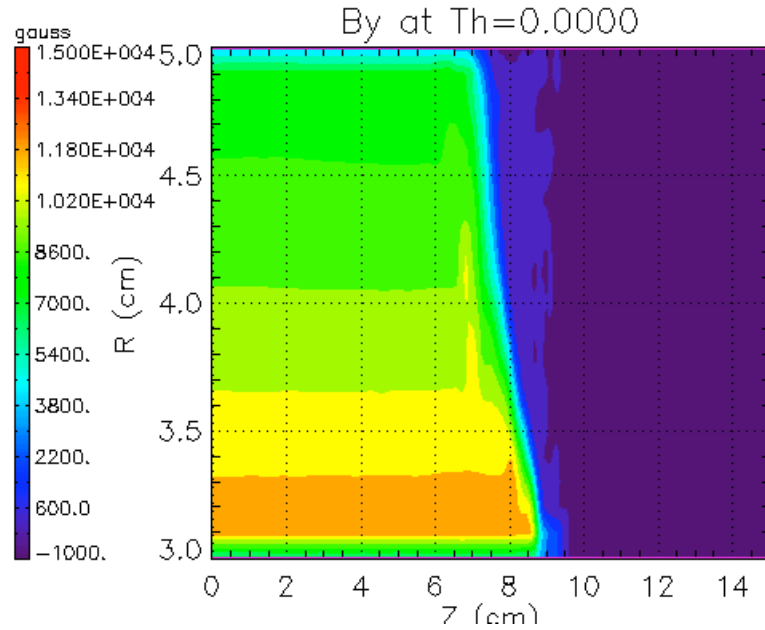
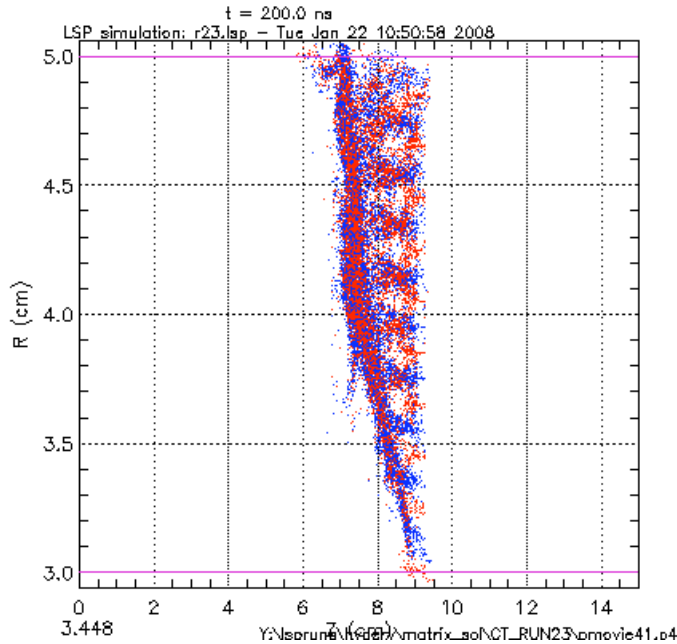
$n_0 = 3 \times 10^{16} \text{ cm}^{-3}$   
 $T_0 = 5 \text{ eV}$   
 $B_\theta \sim 1.2 \text{ T}$



Modified version of “Direct-Implicit” algorithm in Lsp run with large time-step

$$\omega_{pe} \Delta t \sim 40$$

# Plasma Erosion at Anode



$$n_0 = 3 \times 10^{16} \text{ cm}^{-3}$$

$$T_0 = 5 \text{ eV}$$

$$B_\theta \sim 1.2 \text{ T}$$

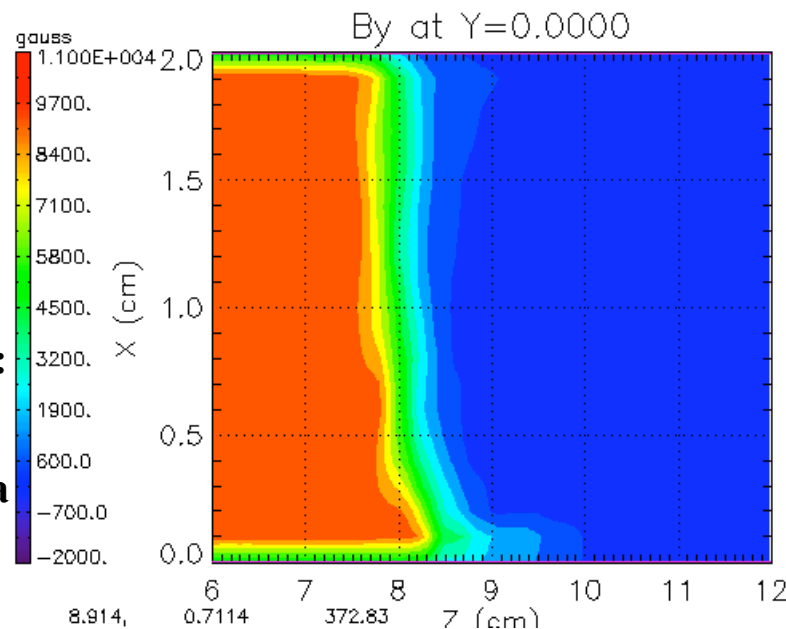
$$B_\theta \approx 1.2 \text{ T}$$

**Thinning of plasma at anode:  
“snowplow” ion acceleration plus  
“blow-by” instability?**

**But similar effect seen in planar  
geometry.**

**Note: Impractical to resolve Debye sheath:  
 $10^{-5} \text{ cm}$  ( $\Delta r = 1 \text{ mm}$ !)**

**Large cell size may increase rate of plasma  
erosion at anode.**

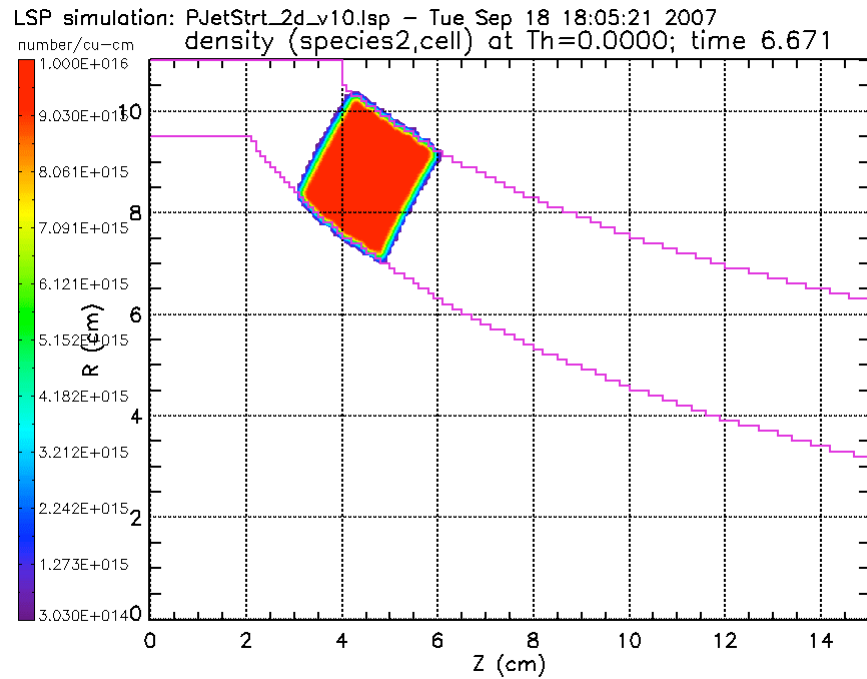


**Planar  
Geometry**

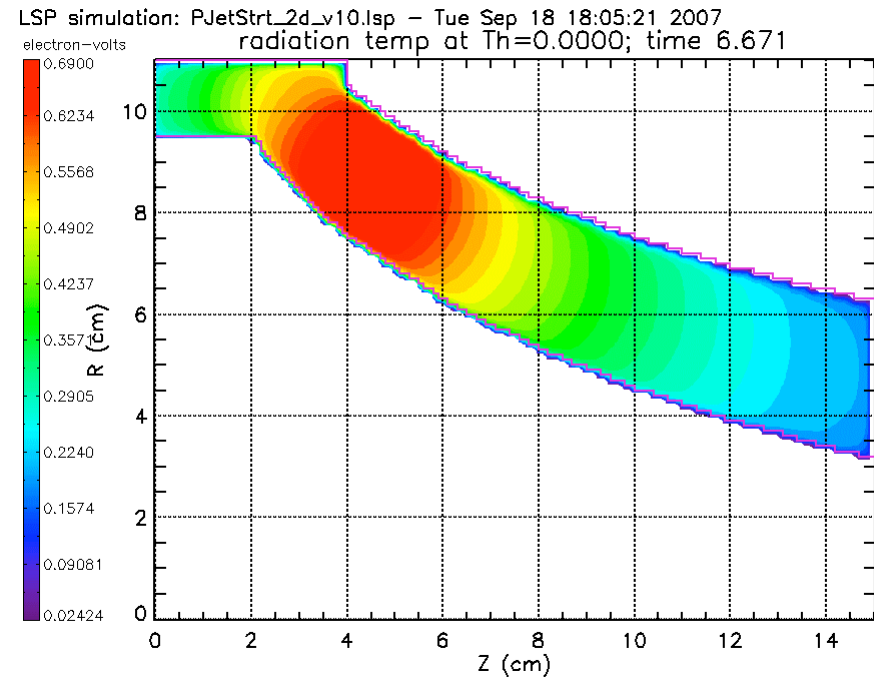
$$B_y = 1 \text{ T}$$

# Work in progress with PCS to access opacity, EOS tables

## CH<sub>2</sub> plasma, 10<sup>16</sup> cm<sup>-3</sup>, 5 eV



## Radiation output



**Multi-group radiation diffusion model ported to LSP and parallelized**

# Summary of Results

Compared EMHD to kinetic-collisional PIC simulation in 1-D for plasma density of  $3 \times 10^{16} \text{ cm}^{-3}$ .

Obtain similar ion dynamics from both algorithms.

Kinetic simulations show strong electron heating at vacuum interface

Significantly increases Hall parameter at interface

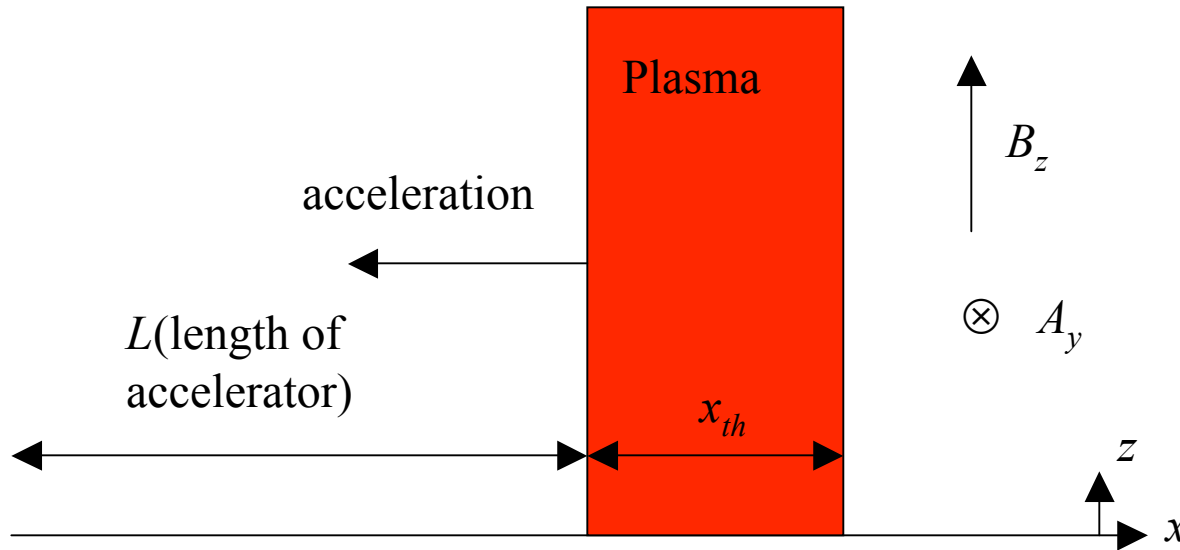
Multi-species jet simulations show mixture remains homogeneous

2D EM coaxial plasma jet simulations feasible but may require mitigation of plasma erosion at electrode surfaces.

In progress with PCS: EOS model to obtain ion charge-states from  $n_i, T_e$



# 1-D plasma jet geometry



Ideal equation of motion:

$$\rho \Delta A x_{th} \frac{dv_x}{dt} = \frac{B_z^2}{2\mu_o} \Delta A$$

Slug acceleration:

$$a = \frac{B_z^2}{2\mu_o \rho x_{th}}$$

Final velocity:

$$v_f = \sqrt{2aL}$$

The time to reach the end  
of the accelerator:

$$t_f = 2L / v_f$$

# Different q/m ions accelerated to same velocity

Estimate of impulse for plasma with (total)  
mass density  $\rho$

$$\Delta v/c \approx 9.4 \times 10^{-12} [\Delta B/G] \left[ \frac{\rho}{\text{g/cm}^3} \right]^{-1/2}$$

$$\Delta B \sim 4 \times 10^4 \text{ G}$$

$$\rho \sim [2 \cdot 2 \times 10^{16} + 12 \cdot 2 \cdot 0.5 \times 10^{16}] m_p \cdot \text{cm}^{-3} = 2.7 \times 10^{-7} \text{ g/cm}^3$$

$$\Delta v/c \sim 0.00073$$

**More massive ions penetrate deeper into the diffusion layer, and experience a larger total force which compensates for their greater inertia.**

